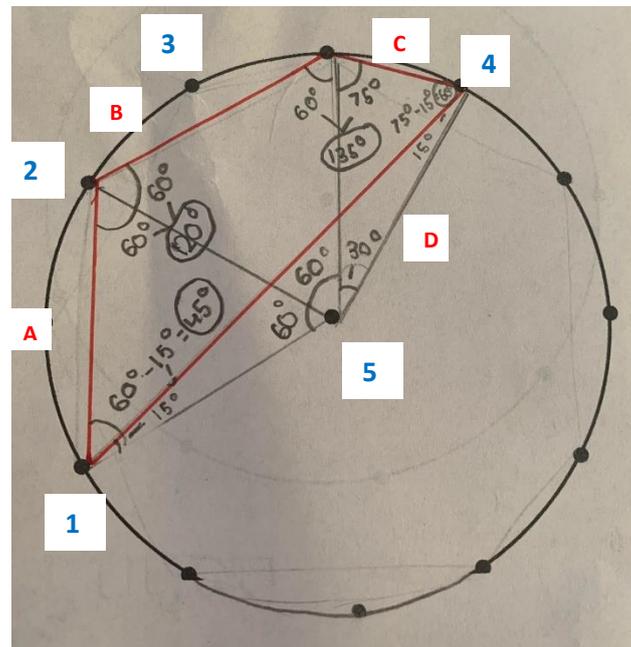


Cyclic Quadrilaterals Proof that the opposite angles still add upto 180° when the center of the circle is not within the quadrilateral.



A,B,C,D: Triangles
1,2,3,4,5: vertices

1. First I connected each vertex of the quadrilateral to the center point.
2. This made 3 isosceles triangles (A,B,C) + 1 another triangle outside the quadrilateral (Triangle D, vertices 154)
3. I calculated the angles at the center point : 60° , 60° and 30°
4. Using these angles I subtracted each of them from 180
 - a. Triangle A: $180 - 60 = 120^\circ$
 - b. Triangle B: $180 - 60 = 120^\circ$
 - c. Triangle C: $180 - 30 = 150^\circ$
5. Then because the 2 base angles are identical as these are isosceles triangles, all I have to do is divide the balance by 2 to get:
 - a. Triangle A: $120/2 = 60^\circ, 60^\circ$
 - b. Triangle B: $120/2 = 60^\circ, 60^\circ$
 - c. Triangle C: $150/2 = 75^\circ, 75^\circ$
6. Triangle D: I used the totals of the angles from the centre (150°) and subtracted them from 180 to get the equal angles of the triangle, which are $15^\circ, 15^\circ$.
7. Finally we calculate the angles:
 - a. Vertex 2: $60^\circ + 60^\circ = 120^\circ$
 - b. Vertex 3: $60^\circ + 75^\circ = 135^\circ$
 - a. Vertex 1: $60^\circ - 15^\circ = 45^\circ$
 - b. Vertex 4: $75^\circ - 15^\circ = 60^\circ$
8. And now that we have found out all the angles for this quadrilateral, we can prove that opposite angles here also add upto 180, even when the

Vertex 2+ Vertex 4: $120^\circ + 60^\circ = 180^\circ$

Vertex 3+ Vertex 1: $135^\circ + 45^\circ = 180^\circ$