

Let the random variable  $X$  represent the number of points gained in a single, randomly selected round of Game 1. Selecting exactly 2 of the four coins to be heads (and the rest consequently being tails), there are  $(4 \text{ choose } 2 =) 6$  states which satisfy the given condition and earn 3 points. The total sample space of results for Game 1 is of size  $(2^4 =) 16$  (each coin is either heads or tails).

$$\begin{aligned} \text{So } E[X] &= 3 \times P(\text{exactly two heads}) \\ &= 3 \times \frac{6}{16} \quad (\text{as each result is equally likely}) \\ &= 1.125 \end{aligned}$$

Let the random variables  $X_1, X_2, X_3$  represent the points gained from spinners 1, 2 and 3, respectively, in a single, randomly selected round of Game 2.

$$\begin{aligned} E[X_1 + X_2 + X_3] &= E[X_1] + E[X_2] + E[X_3] \\ &= \frac{1}{6} \times 2 + \frac{1}{6} \times 2 + \frac{1}{6} \times 2 \\ &= 1 < 1.125 \\ &= E[X] \end{aligned}$$

So the expected earnings in a round of Game 1 are higher than the expected earnings in a round of Game 2. These expectations remain constant between rounds so, as the number of rounds played increases, the ratio of earnings (Game 1 : Game 2) tends towards  $(1.125 : 1)$ . Therefore a wise player ought to favour Game 1 over Game 2.