

Stage 3 ***** Mixed Selection 1 – Solutions

1. Right-angled request

Four right-angled triangles can be drawn in each of the squares, plus four formed from two adjacent sides of the rectangle - that makes 12.

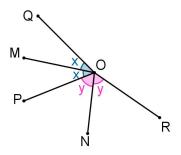
Then there are two right-angled triangles formed by joining the points UQS and PTR.

This makes a total of 14 triangles.

2. Angular reflection

As OQ is the reflection of OP in OM, $\angle QOM = \angle POM$. Similarly, $\angle RON = \angle PON$. Hence, reflex $\angle QOR = 2 \times \angle MON = 260^{\circ}$.

Therefore, $\angle QOR = 360^{\circ} - 260^{\circ} = 100^{\circ}$.



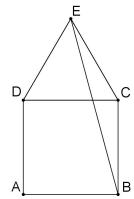
3. Homely angles

Since *ABCD* is a square, $\angle BCD = 90^{\circ}$, and since *CDE* is an equilateral triangle, $\angle DCE = 60^{\circ}$.

Thus $\angle BCE = \angle BCD + \angle DCE = 90^\circ + 60^\circ = 150^\circ$.

Because CDE is an equilateral triangle, EC = DCand also, because ABCD is a square, DC = CB. Hence, EC = CB and ECB is an isosceles triangle.

So
$$\angle CEB = \angle CBE = \frac{1}{2}(180 - 150)^\circ = 15^\circ$$
, and
hence $\angle BED = \angle CED - \angle CEB = 60^\circ - 15^\circ = 45^\circ$.



These problems are adapted from UKMT Mathematical Challenge problems (ukmt.org.uk)



4. Isosceles Meld

Triangle *PQR* is isosceles. Therefore, $\angle PQR = \angle PRQ = 72^{\circ}$. Triangle *PSR* is also isosceles. Therefore, $\angle RPS = \angle RSP = 36^{\circ}$.

Therefore, $x = (180 - 36 - 36)^{\circ} = 108^{\circ}$.

5. Central distance

Each centre is 2.5 cm from the nearer end. So the distance between them is $(9 - (2 \times 2.5))$ cm = 4cm.

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