



Angles, Polygons and Geometrical Proof

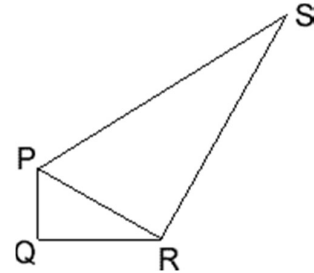
Stage 4 ★★

Mixed Selection 2

1. Two right angles

In the figure above, $PQ = 2\frac{1}{3}$, $PS = 6\frac{6}{7}$, PQR and PRS are right-angled triangles, and the angles QPR and RPS are the same.

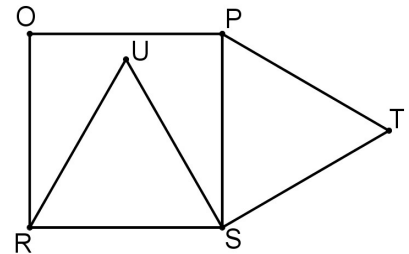
How long is PR ?



2. Internal – external

The diagram shows a square $PQRS$ and two equilateral triangles RSU and PST . PQ has length 1.

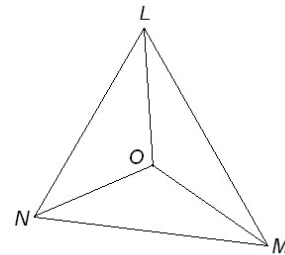
What is the length of TU ?



3. Incentre angle

The three angle bisectors of triangle LMN meet at a point O as shown. We also know $\angle LNM$ is 68° .

What is the size of $\angle LOM$?

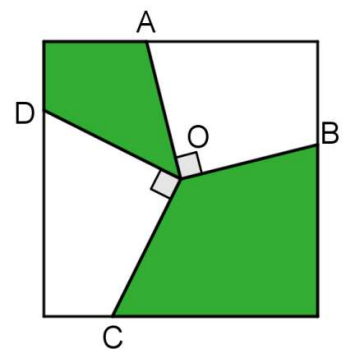


4. Shaded square

The diagram on the right shows a square with side length $2m$ and lines drawn to its sides from its centre O . The points A, B, C and D are all on different sides of the square.

The lines OA and OB are perpendicular, as are OC and OD .

What is the shaded area?



These problems are adapted from UKMT Mathematical Challenge problems (ukmt.org.uk)